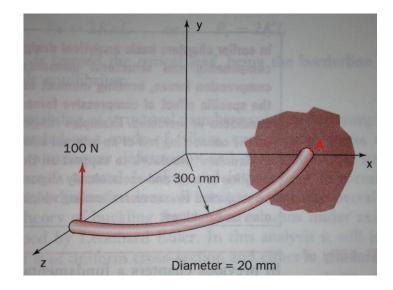
PLEASE NOTE: Answer 3 out of the 4 problems. In case you answer the 4 problems, clearly state which 3 problems you want to be graded.

## Problem 1

A circular section rod has a diameter of 20 mm and the shape of a quadrant of a circle of radius 300 mm, as shown in the figure. The Young's modulus of the material is 208 GPa and the shear modulus is 80 GPa. If a vertical force of 100 N is applied at the free end, determine

- (1) The deflection of the free end in the direction of the force; and
- (2) The stress state at point A which is on the surface of the rod, in the x-y plane, and has a y-coordinate of  $5\sqrt{2}$  mm.

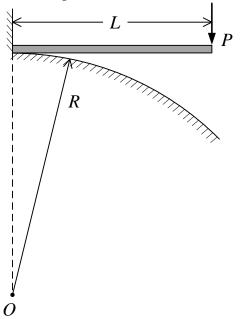


## Problem 2

A cantilever beam of length *L* is clamped at its left end, as shown below. The beam is initially straight, horizontal, and stress free. Underneath the beam there is a cylindrical rigid surface of radius *R*. The top of the cylindrical surface is initially in contact with the left end of the beam. A vertical force, *P*, is applied to the right end of the beam, causing a deflection of  $\delta$  at the right end. The beam has a rectangular cross-section of width *b* and height *h*, and is made of an elastic material with a Young's modulus of *E* and a Poisson's ratio of *v*. Assume *R*>>*L*.

(a). Qualitatively describe the deformation behaviors of the beam when P is increased from zero to infinity.

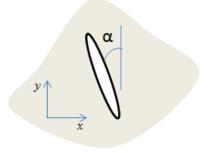
(b). Derive a quantitative relationship between P and  $\delta$ .



## Problem 3

Consider one loading to produce normal stresses on the x-direction of  $\sigma_x = 80$  MPa and  $\sigma_y = -30$  MPa in a brittle material. An additional shear stress is applied. This shear stress increases until a crack is observed to form at an angle of  $\alpha = 20^{\circ}$  (see figure below).

- a) Find shear stress  $\tau_{xy}$  at which cracking occurs.
- b) If this material were loaded in uniaxial tension at what critical stress would fracture occur?



## Problem 4

Consider the cylindrical structure shown made of a rod of *Material A* perfectly adhered to a shell of *Material B*. Both materials are perfectly plastic *Material A* has modulus  $E_A$  and cross sectional area  $A_A$  and *Material B* has modulus  $E_B$  and cross sectional area  $A_B$ . The structure has length  $L_o$ .

A. What is the weight *W* required to deform this structure to the strain  $\varepsilon^*$ , as shown on the Figure?

B. What is the length of the structure after *W* is removed?

C. What are the residual stresses in *Material A* and *Material B* after *W* is removed?

